

# The Alpha and Beta of Risk Attribution

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#### Outline

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- Attributing Risk to Alpha and Beta
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  - Factor Approach
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- Summary

Davis and Menchero, *The Alpha and Beta of Risk Attribution*, Journal of Portfolio Management, Winter 2012, pp. 99-107

# Portfolio Analytics Overview



#### Three Basic Questions of Portfolio Management

Portfolio Managers are concerned with three basic questions:

- 1. How much does an investment decision contribute to <u>return</u>?
- 2. How much does an investment decision contribute to <u>risk</u>?
- 3. How much does an investment decision contribute to risk-adjusted return?

## Segmenting the Portfolio Analytics Space

Return	Risk	Risk/Return	_
Alpha	Risk Forecasting	Portfolio	Future
Modeling	Risk Attribution	Construction	
Performance	Risk Measurement	Risk-adjusted	Past
Attribution	Risk Attribution	Attribution	

#### Risk and Performance Attribution (Ex Post)

$$R_{t} = \sum_{m} Q_{mt}$$
  $Q_{m} = \sum_{t} \beta_{t} Q_{mt} \longrightarrow \begin{bmatrix} R = \sum_{m} Q_{m} \\ Attribution \end{bmatrix}$  Return Attribution

Multi-period linking coefficient (a)

$$\sigma(R) = \sum_{m} \sigma(Q_{m}) \rho(Q_{m}, R)$$

Risk Attribution (b)

- Volatilities and correlations computed using standard time-series methods
  - (a) Menchero, Multi-period Arithmetic Attribution, Financial Analysts Journal, July/Aug 2004, pp 76-91
  - (b) Menchero and Hu, Portfolio Risk Attribution, J. of Performance Measurement, Spring 2006, pp 22-33

#### Risk-Adjusted Attribution (*Ex Post*)

$$\frac{R}{\sigma(R)} = \sum_{m} \left( \frac{\sigma(Q_{m}) \rho(Q_{m}, R)}{\sigma(R)} \right) \left( \frac{Q_{m}}{\sigma(Q_{m}) \rho(Q_{m}, R)} \right)$$
"Risk Weight" "Component IR"

Information Ratio Attribution

- Analyzes each return source on a risk-adjusted basis
- Ideally, every source has the same component Information Ratio
- Answers how efficiently the risk budget was allocated in practice

Menchero, *Risk-adjusted Performance Attribution*, Journal of Performance Measurement, Winter 2006/2007, pp. 22-28

#### Performance Attribution (Ex Ante)

$$R = \sum_{m} x_{m} g_{m}$$

$$\begin{cases} X_{m} = \text{Source Exposure} \\ g_{m} = \text{Source Return} \end{cases}$$

#### **Specific Examples:**

$$R_A = \sum_{n} (w_n^P - w_n^B)(r_n - R_B)$$

**Security Level** 

$$R_{A} = \sum_{i} (w_{i}^{P} - w_{i}^{B})(R_{i}^{B} - R_{B}) + \sum_{i} w_{i}^{P}(R_{i}^{P} - R_{i}^{B})$$

Brinson Model

$$R_A = \sum_k X_k^A f_k + \sum_n w_n^A u_n$$

Factor Approach

#### Risk Attribution (Ex Ante)

$$\sigma(R) = \sum_{m} x_{m} \sigma(g_{m}) \rho(g_{m}, R)$$

Risk Attribution

- Align risk and return attribution variables
- Risk contributions are additive and intuitive
- Identifies three drivers of portfolio risk:
  - Sizes of the exposures  $\mathcal{X}_n$
  - Stand-alone volatilities of the return sources  $\sigma(g_m)$
  - Correlation of return sources with portfolio  $ho(g_m,R)$
- Volatility and correlation forecasts obtained from risk model

Menchero and Davis, "Risk Contribution is Exposure Times Volatility Times Correlation: Decomposing Risk Using the X-Sigma-Rho Formula," Journal of Portfolio Management, Winter 2011, pp. 97-106

#### Information Ratio Attribution (Ex Ante)

$$IR = \frac{R}{\sigma(R)}; \quad R = \sum_{m} x_{m} g_{m}; \quad \sigma(R) = \sum_{m} x_{m} \sigma(g_{m}) \rho(g_{m}, R)$$

$$IR = \sum_{m} \left( \frac{x_{m} \sigma(g_{m}) \rho(g_{m}, R)}{\sigma(R)} \right) \left( \frac{x_{m} g_{m}}{x_{m} \sigma(g_{m}) \rho(g_{m}, R)} \right)$$
"Risk Weight" "Component IR"

- Portfolio IR is the risk-weighted average of component IR
- Component IR is the stand-alone IR of return source, but magnified by  $\rho^{-1}$ . This represents a diversification benefit.

#### **Implied Returns**

For an unconstrained optimal portfolio, each component IR must equal the portfolio IR:

$$IR_{m} = \frac{g_{m}}{\sigma(g_{m})\rho(g_{m},R)} = IR$$

 The expected return of any asset can be "reverse engineered" by computing its volatility and correlation with the optimal portfolio

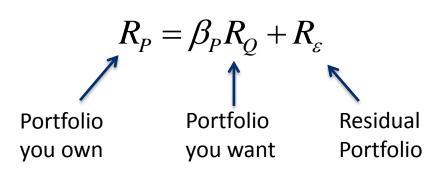
$$E[g_m] = IR \cdot \sigma(g_m) \cdot \rho(g_m, R) = \beta_m \cdot E[R]$$

**Implied Returns** 

- Result reduces to CAPM when the efficient portfolio is the Market
- Constraints reduce the portfolio IR by forcing part of the risk budget to be allocated to low IR positions

#### Residual Volatility and Transfer Coefficient

Investment constraints force the actual portfolio P to deviate from the ideal portfolio Q



- $\sigma_{P}$   $\sigma_{E}$   $\beta_{P} \sigma_{O} = \rho \sigma_{P}$
- Residual portfolio contributes to risk, but not to expected return
- Compute betas and correlations relative to ideal portfolio Q

$$IR_P = \frac{\beta_P R_Q}{\sigma_P} \left( \frac{\sigma_Q}{\sigma_Q} \right)$$

$$\sigma_{\varepsilon} = \sigma_{P} \sqrt{1 - \rho^{2}}$$

Residual Volatility

$$IR_P = \rho \cdot IR_Q$$

Transfer Coefficient

# **Portfolio Optimization**



### **Unconstrained Optimal Portfolios**

Minimize tracking error: 
$$\sum_{mn} w_m^A V_{mn} w_n^A$$

Subject to fixed return constraint: 
$$\sum_{n} w_{n}^{A} r_{n} = 1$$

where: 
$$r_n = \alpha_n + \beta_n R_B$$

$$\mathbf{w}_{A} = \frac{\mathbf{V}^{\text{-1}}\mathbf{r}}{\mathbf{r}'\mathbf{V}^{\text{-1}}\mathbf{r}}$$

Solution: 
$$\mathbf{W_A} = \frac{\mathbf{V^{-1}r}}{\mathbf{r'V^{-1}r}} \qquad \text{Optimal Portfolio} \qquad w_n^A = \frac{\sum_{m} r_m V_{mn}^{-1}}{\sum_{mn} r_m V_{mn}^{-1} r_n}$$

- Optimal portfolio has maximum Information Ratio
- Fixed return constraint determines leverage, does not impact IR
- In general, active weights do not sum to zero
- In general, active beta is non-zero

### **Optimal Portfolios with Constraints**

Fixed return constraint: 
$$\begin{pmatrix} r_1 & r_2 & r_3 & \cdots & r_N \\ 1 & 1 & 1 & \cdots & 1 \\ \beta_1 & \beta_2 & \beta_3 & \cdots & \beta_N \end{pmatrix} \begin{pmatrix} w_1^A \\ w_2^A \\ \vdots \\ w_N^A \end{pmatrix} = \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}$$
 Zero beta constraint: 
$$\begin{pmatrix} r_1 & r_2 & r_3 & \cdots & r_N \\ 1 & 1 & \cdots & 1 \\ \beta_1 & \beta_2 & \beta_3 & \cdots & \beta_N \end{pmatrix} \begin{pmatrix} w_1^A \\ w_2^A \\ \vdots \\ w_N^A \end{pmatrix} = \begin{pmatrix} 1 \\ 0 \\ 0 \end{pmatrix}$$

Minimize tracking error:  $\mathbf{w}_{\mathbf{A}}'\mathbf{V}\mathbf{w}_{\mathbf{A}}$ 

Subject to constraint equation:  $\mathbf{Q}\mathbf{w}_{\mathbf{A}} = \mathbf{c}$ 

Analytic Solution: 
$$\mathbf{w}_{A} = \mathbf{V}^{-1}\mathbf{Q}'(\mathbf{Q}\mathbf{V}^{-1}\mathbf{Q}')^{-1}\mathbf{c}$$

**Optimal Portfolio** 

More complex constraints require numerical solution

# Attributing Risk to Alpha and Beta



### Segmenting Source Returns into Alpha and Beta

$$g_m = g_m^{\alpha} + g_m^{\beta}$$

Decompose Return Source into Alpha and Beta

$$g_m^{\beta} = \beta_m \cdot R_B$$

Beta component is perfectly correlated with the benchmark

$$g_m^{\alpha} = g_m - g_m^{\beta}$$

Alpha component is uncorrelated with the benchmark

$$\sigma(R_A) = \sum_{m} x_m \sigma(g_m^{\alpha}) \rho(g_m^{\alpha}, R_A)$$
 Alpha Risk 
$$+ \sum_{m} x_m \sigma(g_m^{\beta}) \rho(g_m^{\beta}, R_A)$$
 Beta Risk

- Now compute betas relative to benchmark
- Note: active strategy presupposes benchmark is not optimal

#### Example

Portfolio: 95% MSCI World Value Index, with 5% cash (USD)

Benchmark: MSCI World Growth Index

Risk Model: Barra Global Equity Model GEM2L

Analysis Date: September 30, 2009

Portfolio Beta: 1.08

■ Tracking Error: 4.81%

$$R_A = \alpha_P + \beta_A R_B$$

Source	Volatility	Correlation	TE Contrib
Alpha	4.32%	0.90	3.89%
Beta	2.10%	0.44	0.92%
Total	4.81%	1.00	4.81%

■ Assuming optimality and IR=1:  $E[R_B] = (0.92/0.08) = 11.8\%$ 

#### Security Level

Consider bottom-up investment process:

$$R_A = \sum_n w_n^A (r_n - R_B)$$
Active Weight Relative Return

- Relative returns are more appropriate than absolute returns
- Intuitively, we want to overweight the outperformers, but sometimes it is optimal to underweight outperformers (hedging purposes)
- The benchmark represents the risk-free asset (zero relative volatility)
- lacktriangle Cash has relative volatility  $\sigma_{\!\scriptscriptstyle B}$
- Relative return of Cash has correlation of -1.0 to the benchmark

#### **Example: Security Level**

					Alp	ha Compon	ent	Beta	Compone	nt
Asset	Active	Relative	Relative	TE	Relative	Relative	TE	Relative	Relative	TE
Name	Weight	Volatility	Corr	Contrib	Volatility	Corr	Contrib	Volatility	Corr	Contrib
BANK OF AMERICA	1.31%	61.77%	0.44	0.35%	57.12%	0.29	0.22%	23.52%	0.44	0.13%
CITIGROUP	0.69%	82.99%	0.41	0.24%	75.48%	0.25	0.13%	34.49%	0.44	0.10%
GENERAL ELECTRIC	1.56%	35.56%	0.38	0.21%	33.29%	0.25	0.13%	12.48%	0.44	0.08%
JPMORGAN CHASE	1.47%	40.66%	0.37	0.22%	39.32%	0.26	0.15%	10.36%	0.44	0.07%
NESTLE	- <b>1.52</b> %	24.41%	-0.22	0.08%	22.60%	-0.06	0.02%	9.23%	-0.44	0.06%
•••										
UBS	-0.64%	41.47%	0.26	-0.07%	38.49%	0.11	-0.03%	15.44%	0.44	-0.04%
RIO TINTO	-0.57%	47.90%	0.07	-0.02%	43.69%	-0.12	0.03%	19.65%	0.44	-0.05%
EXXON MOBIL	3.00%	23.64%	0.06	0.04%	23.16%	0.15	0.10%	4.72%	-0.44	-0.06%
BHP BILLITON	-1.10%	39.76%	0.01	-0.01%	36.70%	-0.17	0.07%	15.31%	0.44	-0.07%
US Dollar	5.00%	26.78%	-0.44	-0.59%	0.00%	0.00	0.00%	26.78%	-0.44	-0.59%
Total				4.81%			3.89%			0.92%

- Assuming optimality and IR=1, expected return of benchmark is (26.78)(0.44), or 11.8 percent
- GE is expected to outperform benchmark by (35.56)x(0.38), or 13.5 percent
- Portfolio is underweight UBS, although it has a positive expected return
- US Dollar is the greatest diversifier and contributes zero to Alpha risk

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#### **Example: Sector-Based Approach**

$$R = \sum_{i} (w_{i}^{P} - w_{i}^{B})(R_{i}^{B} - R_{B}) + \sum_{i} w_{i}^{P}(R_{i}^{P} - R_{i}^{B})$$

Sector	Portfolio	Bench	Active	Relative	Relative	Allocation	Active	Active	Selection	Total
Name	Weight	Weight	Weight	Volatility	Corr	<b>TE Contrib</b>	Volatility	Corr	<b>TE Contrib</b>	TE Contrib
Energy	13.09%	7.77%	5.32%	18.04%	0.13	0.12%	12.64%	-0.02	-0.03%	0.09%
Materials	4.98%	8.80%	-3.82%	17.09%	0.02	-0.01%	12.09%	0.41	0.25%	0.23%
Industrials	10.55%	9.85%	0.70%	5.80%	0.32	0.01%	7.84%	0.45	0.38%	0.39%
Cons Disc	6.97%	11.27%	-4.31%	7.50%	0.30	-0.10%	6.44%	0.25	0.11%	0.01%
Cons Stpls	4.39%	15.65%	-11.25%	10.21%	-0.25	0.29%	6.86%	0.24	0.07%	0.36%
<b>Health Care</b>	6.53%	13.49%	-6.96%	11.02%	-0.32	0.25%	8.15%	0.26	0.14%	0.38%
Financials	32.57%	8.39%	24.19%	12.30%	0.58	1.73%	9.61%	0.57	1.78%	3.50%
IT	3.25%	19.95%	-16.70%	9.22%	-0.16	0.25%	10.34%	0.08	0.03%	0.28%
Telecom	5.95%	2.58%	3.36%	14.16%	-0.02	-0.01%	14.39%	0.10	0.09%	0.08%
Utilities	6.72%	2.26%	4.47%	13.92%	-0.17	-0.10%	9.28%	0.25	0.16%	0.05%
Cash	5.00%	0.00%	5.00%	26.78%	-0.44	-0.59%	0.00%	0.00	0.00%	-0.59%
Total	100.00%	100.00%	0.00%	3.94%	0.47	1.84%	4.57%	0.65	2.96%	4.81%

- Financial sector contributes 350 bps to TE; 173 bps due to Allocation
- Each attribution effect can be subdivided into Alpha and Beta components

## Alpha Decomposition for Brinson Model

					Alpha (Residual) Component					
Sector	Portfolio	Bench	Active	Relative	Relative	Allocation	Active	Active	Selection	Total
Name	Weight	Weight	Weight	Volatility	Corr	TE Contrib	Volatility	Corr	TE Contrib	TE Contrib
Energy	13.09%	7.77%	5.32%	15.95%	-0.09	-0.07%	10.77%	0.25	0.35%	0.28%
Materials	4.98%	8.80%	-3.82%	15.11%	-0.21	0.12%	11.89%	0.34	0.20%	0.32%
Industrials	10.55%	9.85%	0.70%	5.61%	0.22	0.01%	6.93%	0.28	0.21%	0.22%
Cons Disc	6.97%	<b>11.27</b> %	-4.31%	7.29%	0.20	-0.06%	6.18%	0.13	0.06%	-0.01%
Cons Stpls	4.39%	15.65%	-11.25%	7.48%	0.06	-0.05%	6.83%	0.20	0.06%	0.01%
<b>Health Care</b>	6.53%	13.49%	-6.96%	8.95%	-0.08	0.05%	8.11%	0.30	0.16%	0.21%
Financials	32.57%	8.39%	24.19%	10.69%	0.42	1.08%	8.64%	0.42	1.18%	2.26%
IT	3.25%	19.95%	-16.70%	9.22%	-0.16	0.25%	10.34%	0.07	0.02%	0.27%
Telecom	5.95%	2.58%	3.36%	13.78%	0.08	0.04%	14.26%	0.16	0.14%	0.18%
Utilities	6.72%	2.26%	4.47%	11.73%	0.08	0.04%	9.13%	0.17	0.11%	0.15%
Cash	5.00%	0.00%	5.00%	0.00%	-0.31	0.00%	0.00%	0.00	0.00%	0.00%
Total	100.00%	100.00%	0.00%	3.81%	0.37	1.41%	4.43%	0.56	2.48%	3.89%

Alpha component contributes 108 bps (of 173 bps total) to Financials Allocation

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#### Beta Decomposition for Brinson Model

					Beta (Market Timing) Component					
Sector	Portfolio	Bench	Active	Relative	Relative	Allocation	Active	Active	Selection	Total
Name	Weight	Weight	Weight	Volatility	Corr	TE Contrib	Volatility	Corr	TE Contrib	TE Contrib
Energy	13.09%	7.77%	5.32%	8.44%	0.44	0.20%	6.61%	-0.44	-0.38%	-0.18%
Materials	4.98%	8.80%	-3.82%	7.98%	0.44	-0.13%	2.15%	0.44	0.05%	-0.09%
Industrials	10.55%	9.85%	0.70%	1.46%	0.44	0.00%	3.66%	0.44	0.17%	0.17%
Cons Disc	6.97%	11.27%	-4.31%	1.78%	0.44	-0.03%	1.81%	0.44	0.06%	0.02%
Cons Stpls	4.39%	15.65%	-11.25%	6.94%	-0.44	0.34%	0.55%	0.44	0.01%	0.35%
<b>Health Care</b>	6.53%	13.49%	-6.96%	6.42%	-0.44	0.20%	0.75%	-0.44	-0.02%	0.17%
Financials	32.57%	8.39%	24.19%	6.08%	0.44	0.64%	4.20%	0.44	0.60%	1.24%
IT	3.25%	19.95%	-16.70%	0.03%	-0.44	0.00%	0.22%	0.44	0.00%	0.01%
Telecom	5.95%	2.58%	3.36%	3.29%	-0.44	-0.05%	1.88%	-0.44	-0.05%	-0.10%
Utilities	6.72%	2.26%	4.47%	7.50%	-0.44	-0.15%	1.69%	0.44	0.05%	-0.10%
Cash	5.00%	0.00%	5.00%	26.78%	-0.44	-0.59%	0.00%	0.00	0.00%	-0.59%
Total	100.00%	100.00%	0.00%	1.00%	0.44	0.44%	1.11%	0.44	0.48%	0.92%

- Beta component contributes 64 bps (of 173 bps total) to Financials Allocation
- Correlation between benchmark and active portfolio is 0.44

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#### Factor-Based Approach

- Attribute risk to a set of custom factors:
  - World factor
  - 10 GICS Economic Sectors

$$R = \sum_{k} X_{k}^{P} f_{k} + \sum_{n} w_{n} u_{n}$$

- Use Predicted Beta as a style factor, together with Value, Size, and Momentum
- Style factors are cap-weighted mean zero
- Use benchmark as estimation universe
- Use benchmark cap-weights as regression weights
- All factor portfolios (except Beta and World) have zero beta
- World factor portfolio becomes the benchmark (beta=1)
- Beta factor portfolio is dollar neutral (also with beta=1)

Menchero and Poduri, *Custom Factor Attribution*, Financial Analysts Journal, March/April 2008, pp. 81-92

#### **Example: Factor-Based Approach**

					Alpl	na Compor	nent	Bet	a Compon	ent
	Active			TE			TE			TE
Source	Exposure	Volatility	Corr	Contrib	Volatility	Corr	Contrib	Volatility	Corr	Contrib
World	-0.05	26.78%	0.44	-0.59%	0.00%	-0.28	0.00%	26.78%	0.44	-0.59%
Energy	0.05	16.20%	-0.08	-0.07%	16.20%	-0.08	-0.07%	0.00%	-0.44	0.00%
Materials	-0.04	14.59%	-0.20	0.11%	14.59%	-0.20	0.11%	0.00%	0.44	0.00%
Industrials	0.01	5.34%	0.20	0.01%	5.34%	0.20	0.01%	0.00%	0.44	0.00%
ConsDscr	-0.04	7.30%	0.22	-0.07%	7.30%	0.22	-0.07%	0.00%	-0.44	0.00%
ConsStpls	-0.11	7.17%	0.03	-0.03%	7.17%	0.03	-0.03%	0.00%	-0.44	0.00%
HealthCare	-0.07	8.89%	-0.12	0.07%	8.89%	-0.12	0.07%	0.00%	-0.44	0.00%
Financials	0.24	11.92%	0.40	1.15%	11.92%	0.40	1.15%	0.00%	0.44	0.00%
IT	-0.17	9.12%	-0.13	0.20%	9.12%	-0.13	0.20%	0.00%	0.44	0.00%
Telecom	0.03	14.07%	0.06	0.03%	14.07%	0.06	0.03%	0.00%	0.44	0.00%
Utilities	0.04	10.62%	0.00	0.00%	10.62%	0.00	0.00%	0.00%	0.44	0.00%
Momentum	0.05	6.28%	-0.12	-0.04%	6.28%	-0.12	-0.04%	0.00%	-0.44	0.00%
Beta	0.13	31.57%	0.36	1.48%	16.72%	-0.01	-0.03%	26.78%	0.44	1.51%
Value	0.48	4.74%	0.14	0.32%	4.74%	0.14	0.32%	0.00%	0.44	0.00%
Size	0.07	3.05%	-0.13	-0.03%	3.05%	-0.13	-0.03%	0.00%	-0.44	0.00%
Specific	1.00	4.02%	0.56	2.27%	4.02%	0.56	2.27%	0.00%	-0.44	0.00%
Total				4.81%			3.89%			0.92%

- Beta risk is fully explained by Beta and World factors
- World factor accounts for hedging due to cash position (-59 bps)
- Beta factor portfolio contains some residual risk

## Residual Weights versus Residual Returns



#### Alpha Analysis: Residual Weights or Residual Returns?

- Our approach is based on active weights and residual returns
  - Active weights are intuitive
  - Residual returns are uncorrelated with the benchmark
- Alternative approach: use residual weights with total returns
- This adds up to the total portfolio alpha:

$$\sum_{n} \left( w_{n}^{P} - \beta_{P} w_{n}^{B} \right) \left( \alpha_{n} + \beta_{n} R_{B} \right) = \alpha_{P}$$
Residual Weight Total Return

Residual Weights Approach

- Shortcomings:
  - Residual weights are less intuitive
  - Total returns are correlated with the benchmark
  - Inconsistent with notion of Alpha as an uncorrelated return source

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#### **Example: Residual Exposures**

Source	Residual Exposure	Factor Volatility	Corr	TE Contrib
World	-0.13	26.78%	0.44	-1.51%
Energy	0.05	16.20%	-0.08	-0.06%
Materials	-0.05	14.59%	-0.20	0.13%
Industrials	0.00	5.34%	0.20	0.00%
ConsDscr	-0.05	7.30%	0.22	-0.08%
ConsStpls	-0.12	7.17%	0.03	-0.03%
HealthCare	-0.08	8.89%	-0.12	0.08%
Financials	0.24	11.92%	0.40	1.12%
IT	-0.18	9.12%	-0.13	0.22%
Telecom	0.03	14.07%	0.06	0.03%
Utilities	0.04	10.62%	0.00	0.00%
Momentum	0.05	6.28%	-0.12	-0.04%
Beta	0.13	31.57%	0.36	1.48%
Value	0.48	4.74%	0.14	0.32%
Size	0.07	3.05%	-0.13	-0.03%
Specific	1.00	4.02%	0.56	2.27%
Total				3.89%

- Factor exposures are quoted on a residual basis
- World and Beta factors make nonintuitive contribution to Alpha risk

$$X_k^R = \sum_n w_n^R X_{nk}$$
 Residual Exposures

msci.com

#### **Summary**

- Portfolio returns can always be segmented into Alpha and Beta:
  - Alpha component is uncorrelated with the benchmark
  - Beta component is perfectly correlated with the benchmark
- Portfolio risk can always be segmented into Alpha and Beta sources
- Three examples:
  - Security Level
  - Brinson Model
  - Factor Approach
- Alternative formulation based on residual weights leads to non-intuitive results

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